

Adsorption isotherms, kinetic and thermodynamic studies for cadmium and lead ions from water solutions using Amberlyst 15 resin

Adalet TUNÇELİ, Abdullah ULAŞ, Orhan ACAR*, Ali Rehber TÜRKER

Department of Chemistry, Faculty of Science, Gazi University, Ankara Turkey

*Correspondence: oacar@gazi.edu.tr

ORCIDs:

Adalet TUNÇELİ: <https://orcid.org/0000-0001-6927-0496>

Abdullah ULAŞ: <https://orcid.org/0000-0003-4512-1458>

Orhan ACAR: <https://orcid.org/0000-0002-0969-2627>

Ali Rehber TÜRKER: <https://orcid.org/0000-0001-7442-105X>

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Abstract: Adsorption isotherms, kinetic and thermodynamic parameters for Cd(II) and Pb(II) ions in water solutions by using Amberlyst 15 resin were performed and evaluated by utilizing solid phase extraction method with batch system at 298, 308 and 318 K. Flame atomic absorption spectrometry was utilized for absorbance measurements of Cd and Pb in solutions. The Langmuir, Freundlich and Dubinin–Radushkevich isotherm models, respectively were implemented to equilibrium results obtained. Experimental and theoretical monolayer adsorption capacities of resin for adsorptions of Cd(II) and Pb(II) by the Langmuir isotherm model were approximately the same and they were 120 and 116 mg/g for Cd(II) and Pb(II) ions, respectively at 318 K. Most appropriate kinetic model for adsorption of Cd(II) and Pb(II) on the resin was found as pseudo-second-order. Contact time and temperature for adsorption of analytes on the resin were optimized as 45 min and 298 K. Activation energies (E_a) and thermodynamic values (ΔG° , ΔH° and ΔS°) were determined and assessed. Results showed that adsorptions of Cd(II) and Pb(II) on Amberlyst 15 were spontaneous, exothermic and chemical ion-exchange process.

Keywords: Cadmium, Lead, Amberlyst 15 resin, Adsorption, Thermodynamic parameters

1. Introduction

Development of industry and increase in population have created rapid increase in environmental pollutions over the years. The presence of Cd and Pb metal ions in water samples can create serious environmental and human health problems because of their highly toxic effects even if at low concentrations. Some industrial areas of the use of cadmium and lead are electroplating, mining, painting, corrosion, nuclear reactor control systems, radiation protection from x-ray, battery manufacturing industries and etc [1, 2]. Their sources are also agricultural and industrial wastewaters, rivers, lakes,

dams and seas [3]. Waters containing these metal ions are extremely unsuitable for human beings when taken by the human body. Some of the health problems caused by cadmium and lead are high blood pressure, lung and prostate cancer, anemia, the collapse of nervous and immune systems, kidney function disturbances and brain damage [1–7]. Therefore, determinations of these metal ions from natural and waste waters are important to protect environment and human health.

Separation and pre-concentration methods such as liquid-liquid extraction [8-13], cloud point extraction [10-12], co-precipitation [13], adsorption by solid phase extraction (SPE) [14-19] and solid phase micro extraction [20], ion-exchange [21, 22], single drop micro-extraction [23] and etc. were used for the determination of Cd and Pb when concentrations of them were below detection limits. After application of these methods, various analytical techniques such as graphite furnace atomic absorption spectrometry (GFAAS) [24-26], inductively coupled plasma mass spectrometry (ICP-MS) [27] and inductively coupled plasma optical emission spectrometry (ICP-OES) [28] and flame atomic absorption spectrometry (FAAS) were used [8, 10-12, 15-19, 21]. Among them, the SPE technique was mostly used for separation or pre-concentration of trace metal ions and FAAS was one of the most useful techniques used because of its high sensitivity and selectivity. Many studies have been carried out for determination of Cd and Pb in several samples such as waters, foods, biological and environmental samples by GFAAS and FAAS with various adsorbents [14, 16, 24]. Besides determination studies, many methods have been developed to preconcentrate Cd(II) and Pb(II) ions in the environments [18, 19, 21, 29-33]. In recoveries of Cd(II) and Pb(II) ions, macromolecular styrene divinylbenzene based synthetic materials [21, 29-31], bacteria

[3, 32], yeast [33, 34], various plant shells [35, 36], seaweed [37] and nano-size materials have been used as adsorbents [15, 38, 39].

The aims of this work were to perform adsorption isotherms, kinetics and thermodynamic parameters for Cd(II) and Pb(II) ions by utilizing Amberlyst 15 resin as an adsorbent [40-42]. Kinetics, reaction orders, adsorption capacities, contact times and thermodynamic values (ΔG° , ΔH° , ΔS°) at 298, 308 and 318 K, respectively and E_a were determined for both Cd(II) and Pb(II) ions. Amberlyst 15 has a strong ion-exchange resin including sulfonic acid, styrene divinylbenzene groups and H^+ form. The results of this study will help researchers to use the adsorbent for solid phase extraction of the analytes for analytical method development.

2. Materials and methods

2.1. Chemicals and reagents

All chemicals and reagents utilized were of analytical grade. Ultrapure water (resistivity was about 18.3 M Ω cm) was utilized in experiments. Solutions were obtained by dissolving metal salts including nitrates. HCl (37%, m/m), HNO₃ (65%, m/m), NaOH, methanol and metal salts utilized in experiments were taken from Merck (Darmstadt, Germany). The laboratory glassware and polyethylene bottles were kept in nitric acid solution (10%, v/v) at an overnight, rinsed thoroughly with ultrapure water and dried before using. Standard stock solutions of Cd(II) and Pb(II) (1000 mg/L for each) were obtained by dissolving 0.28 g of Cd(NO₃)₂·4H₂O and 0.16 g of Pb(NO₃)₂ (Merck) in 0.1 mol/L HNO₃ solution and poured in polyethylene bottles. Solutions of Cd(II) and Pb(II) (100 mg/L for each) and working calibration solutions (0.5 – 5.0 mg/L for each element) were prepared by diluting stock solutions before using. Nitric acid and hydrochloric acid solutions (0.1, 0.5, 1.0 and 2.0 mol/L) were prepared by diluting

gently concentrated HNO_3 and concentrated HCl with ultrapure water, respectively. The NaOH solution (0.1 mol/L) was prepared by dissolving 2.01 g NaOH in enough ultrapure water and diluted to 500 mL.

Amberlyst 15 resin which has cross-linked styrene divinylbenzene copolymer has been taken from Rohm and Haas (Philadelphia, USA). It has some features such as strongly sulfonic acid functional groups ($-\text{SO}_3\text{H}$), ionic H^+ structure, 0 - 14 workable pH range, $53 \text{ m}^2/\text{g}$ surface area, 300 nm average pore diameter, 400 - 500 μm particle size, 1 – 120 $^\circ\text{C}$ temperature range and beads physical structure [42]. The resin was washed by utilizing 1 mol/L HCl solution, methanol and ultrapure water, respectively for regeneration and to remove unreacted monomers and impurities in the structure. After drying for 4 h at 70 $^\circ\text{C}$, it was utilized in experiments.

2.2. Instruments

Varian AAS240FS Model flame atomic absorption spectrometry (Palo Alto, USA) equipped with a deuterium lamp for background correction was utilized for determinations of Cd and Pb according to recommended conditions by the manufacturer. Operating conditions of Varian Cd and Pb lamps were 4 mA and 228.8 nm for Cd and 10 mA and 283.3 nm for Pb, respectively. Spectral band passes (0.7 nm) and acetylene/air flow rates (1.4/ 13.6 L/min) were utilized for both elements. WTW 720 model pH meter (glass electrode) (Weilheim, Germany) was utilized for all pH measurements. A thermostatic water bath shaker (Nuve ST 402, Turkey) equipped with 150 rpm fixed speed and adjusted suitable temperatures as 298, 308 and 318 K was utilized for kinetic studies.

2.3. Batch adsorption studies

Batch equilibrium method was performed to determine adsorption isotherms, contact times, temperatures, initial concentrations, kinetics and thermodynamic parameters of Cd(II) and Pb(II) ions on Amberlyst 15. Batch equilibrium studies were carried out utilizing 50 mL of 0.2 mg/L Cd(II) or 50 mL of 0.2 mg/L Pb(II) standard solution, separately in 100 mL flask containing about 50 mg of resin. pH values of solutions were adjusted to 2 - 10 range utilizing 0.1 mol/L HCl and 0.1 mol/L NaOH solutions. Flasks were put onto mechanical shaker and mixed for 120 min at adjusted temperature. The suspensions in elution solutions were filtered and concentrations of Cd(II) and Pb(II) in elutions were determined by FAAS after required dilutions. Maximum analyte mass adsorbed per mass of resin was obtained at pH = 4.0 for both Cd(II) and Pb(II) [43]. Then, range of initial concentrations of Cd(II) and Pb(II) solutions varied from 25 to 1000 mg/L in 50 mL solutions were prepared. Each solution was poured into 100 mL volumetric flask containing about 50 mg of resin, separately and pH value was adjusted to 4.0. The same procedure given above was used for all solutions and concentrations of analytes were determined by FAAS to investigate the mass of analyte ion adsorbed by the resin. Adsorbed analyte amount per unit mass of resin at equilibrium q_e (mg/g) was obtained by utilizing equation (1):

$$q_e = \frac{(C_o - C_e) \cdot V}{m}$$

(1)

where, C_o and C_e are initial and equilibrium concentrations of Cd(II) and Pb(II) (mg/L), respectively. V is solution volume (L) and m is resin mass (g). For isotherm studies, all experiments were repeated three times at 298, 308 and 318 K temperatures with range of initial concentrations of Cd(II) and Pb(II) ions in solutions as given above. Kinetic

data were obtained from these three different temperatures for both Pb(II) and Cd(II) ions.

3. Results and Discussion

3.1. Adsorption isotherms and capacities

Adsorption isotherms play important roles for adsorbents in adsorption systems and they provide maximum adsorption capacity for metal ions from solutions. Adsorption continues until an equilibrium between concentration of analyte retained on surface of adsorbent and concentration of analyte in solution is established [34]. A batch method was utilized to determine initial concentrations of Cd(II) and Pb(II) on adsorption capacity of resin at pH value 4.0 and at 298, 308 and 318 K temperatures. Average values of three replicate measurements of results with standard deviation (less than 4%) were depicted in Figure 1. As seen in Figure 1, adsorption capacity of resin increased by increasing initial concentrations of Cd(II) or Pb(II) until the equilibrium was obtained. Initial metal concentration ensures driving force to accomplish mass transfer of ion between aqueous solution and solid phase [44]. When initial analyte concentration was increased up to approximately 400 mg/L, adsorption equilibrium capacity increased. Experimental equilibrium adsorption capacities (q_e) of resin for Cd(II) and Pb(II) ions at different temperatures calculated by equation (1) were dedicated in Table 1. As seen in Table 1, they were in range of 120 – 149 mg/g for Cd and 116 – 152 mg/g for Pb, respectively and they decreased by increasing temperature.

The Langmuir, Freundlich and Dubinin-Radushkevich (D-R) isotherm models were most commonly utilized isotherms to explain adsorption equilibrium isotherms experimentally and mathematically. According to the Langmuir theory, every

adsorption occurs on monolayer homogenous sites of adsorbent until saturated adsorption to be reached [1-3, 41, 44]. Linearized form of the Langmuir isotherm model was explained by utilizing equation (2):

$$\frac{C_e}{q_e} = \frac{1}{K_L q_m} + \frac{C_e}{q_m}$$

(2)

where, C_e is equilibrium concentration of analyte in eluent (mg/L), q_e is mass of analyte ion adsorbed per resin mass at equilibrium (mg/g), q_m is adsorption capacity of adsorbent (mg/g) and K_L (L/mg) is adsorption constant of the Langmuir isotherm model related to free energy of adsorption. Plots of C_e/q_e versus C_e values for Cd(II) and Pb(II) obtained at 298 K were depicted in Figure 2 as an example. Average values of q_m and K_L theoretically obtained from the slope ($1/q_m$) and intercept ($1/(K_L q_m)$) by using linearized Langmuir isotherm model [44] at 298, 308 and 318 K, respectively were dedicated in Table 1. As seen in Table 1, when temperature was increased, q_m values decreased, but theoretically calculated q_m values were similar with experimental q_e values for both Cd(II) and Pb(II) at 318 K. Increasing q_m value with decreasing temperature demonstrated that the adsorption process was exothermic. K_L values found for adsorptions of both Pb(II) and Cd(II) at three different temperatures were approximately the same. This means that the resin has similar affinity towards to Pb(II) and Cd(II) since K_L value is directly proportional to the binding energy [45].

In addition, dimensionless resolution factor or equilibrium parameter (R_L) can be calculated to determine suitability of adsorption process and essential characteristics of the Langmuir isotherm model. According to R_L value given by using equation (3), isotherm shape may be utilized to predict whether adsorption system is preferable or non preferable.

$$R_L = \frac{1}{1 + K_L C_o}$$

(3)

where, C_o is initial concentrations of Cd(II) and Pb(II) (mg/L) and K_L is the Langmuir constant described above and given in Table 1. Four probabilities of the R_L values to indicate the shapes of adsorption isotherms are suitable ($0 < R_L < 1$), unsuitable ($R_L > 1$), linear ($R_L = 1$) or irreversible ($R_L = 0$) [34, 43, 45]. In this study, ranges of R_L values calculated for all initial concentrations (25 - 1000 mg/L) were from 0.02 to 0.51 for Cd and from 0.02 to 0.59 for Pb, respectively at 298, 308 and 318 K temperatures. These values demonstrated that adsorptions of Cd(II) and Pb(II) ions on the resin at each temperature were favorable.

The Freundlich isotherm model can be applied to heterogeneous adsorption surface and active sites of the resin with different energy. Using of this isotherm model for heterogeneous system is better than the Langmuir isotherm model [44, 46]. Linearized Freundlich model was explained by equation (4):

$$\log q_e = \log K_F + \left(\frac{1}{n}\right) \log C_e$$

(4)

where, K_F is adsorption capacity of resin (mg/g) and $1/n$ is an adsorption intensity. If $0 < 1/n < 1$ - adsorption is suitable, $1/n = 0$ - irreversible and $1/n = 1$ - unsuitable. K_F and n values obtained from intercept and slope of the straight lines at 298, 308 and 318 K were dedicated in Table 1. As seen in Table 1, K_F values theoretically found were smaller than the values (q_m) from Langmuir isotherm model and the experimental values (q_e). As seen in Figure 2 and Table 1, the Langmuir model is more suitable than

the Freundlich model by comparing correlation coefficients (R^2) at 298, 308 and 318 K and monolayer adsorption of Cd(II) and Pb(II) on resin is favorable.

The Dubinin - Radushkevich (D - R) isotherm model was utilized to determine whether adsorption process was physical or chemical ion exchange [22, 41, 46]. Adsorption free energy (E) was obtained by using the D-R model. Experimental data were also implemented to linear form of D - R isotherm model given by equation (5):

$$\ln q_e = \ln q_m - \beta \varepsilon^2 \quad (5)$$

where, q_e is mol of analyte ion adsorbed per mass of adsorbent (mol/g), q_m is adsorption capacity (mol/g), β is activity coefficient related to the mean free energy of adsorption (mol^2/J^2) and ε is the Polanyi potential associated with the maximum adsorption capacity at equilibrium and it can be obtained by using equation (6):

$$\varepsilon = RT \ln \left(1 + \frac{1}{C_e} \right) \quad (6)$$

where T is temperature (K), R is international gas constant (8.314 J/(mol·K)) and C_e is metal ion concentration (mol/L) at equilibrium, respectively. Plots of $\ln q_e$ versus ε^2 values for Cd(II) and Pb(II) ions obtained by equation (5) at 298 K were depicted in Figure 3 as an example. The q_m and β values were obtained from intercept and slope for each plot at 298, 308 and 318 K, respectively and q_m values obtained were dedicated in Table 1. As shown in Table 1, q_m values obtained from D - R isotherm model for Cd(II) and Pb(II) reduced by increasing temperature of solution. This was explained that process was exothermic.

The free energy difference between adsorbed surface of resin and saturated liquid concentration of element ions to be adsorbed was explained as adsorption potential by

the Polanyi and by Dubinin [47]. Average free energy E (kJ/mol) for adsorption was given by utilizing equation (7):

$$E = \frac{1}{\sqrt{-2\beta}}$$

(7)

The E value obtained explains the information about whether adsorption mechanism is physical or chemical ion - exchange. If $8 \text{ kJ/mol} \leq E \leq 16 \text{ kJ/mol}$, adsorption process is chemical ion – exchange. If E is lower than 8 kJ/mol , adsorption process is physical exchange [48]. Average adsorption free energies of Cd and Pb at 298 K, 308 K and 318 K calculated were dedicated in Table 1. As dedicated in Table 1, E values found were 12.31 - 13.36 kJ/mol for Cd and 13.61 - 15.08 kJ/mol for Pb and mechanism of adsorption process was chemical ion exchange.

3.2. Comparison of adsorption capacities of resin with literature values

Maximum adsorption capacity (q_m) values of Amberlyst 15 resin for recoveries of Cd (II) and Pb (II) ions obtained from the Langmuir isotherm model (Table 1) were compared with previously reported literature values on different types of adsorbents [49-56]. They were dedicated in Table 2. As seen in Table 2, q_m values were widely different from each other because the experiments studied were carried out under different conditions such as pH of solution, initial concentration of element and adsorbent preparation. The q_m values of the resin for Cd (II) ion obtained at three different temperatures were within the previous studies [49, 51]. The q_m values for Pb (II) ion were similar with the result obtained from Oxidized MWCNTs adsorbent [56].

3.3. Chi-square (X^2) analysis

The X^2 analysis was an important information about suitability of isotherm model [46, 57] and it was performed to identify suitable isotherm model for explaining adsorptions

of Cd(II) and Pb(II) ions on Amberlyst 15 resin from aqueous solutions. The mathematical explanation of the X^2 analysis was given by equation (8):

$$X^2 = \sum (q_e - q_m)^2 / q_m \quad (8)$$

where q_e and q_m are experimental equilibrium and theoretical equilibrium adsorption capacities calculated from the models (mg/g), respectively. If calculated data from a model are close to experimental data, X^2 will be low. If they are different, X^2 will be a high number. As seen in Table 1, when temperature of solution was increased for the Langmuir isotherm model, difference between q_e and q_m values for both Cd(II) and Pb(II) decreased and the X^2 values were near to zero. Therefore, the Langmuir isotherm model was suitable isotherm model for adsorption process proposed. When correlation coefficients (R^2) of isotherm models for Cd(II) and Pb(II) ions obtained were compared, R^2 values found from the Langmuir model were about 1.0 and higher than R^2 values from other isotherm models.

3.4. Adsorption kinetics

Orders of kinetic reactions for adsorption of Cd(II) and Pb(II) ions on Amberlyst 15 resin were investigated. For this purpose, adsorptions of initial concentrations of Cd(II) and Pb(II) on resin were studied, respectively. Nearly 400 mg/L Cd(II) and Pb(II) initial concentrations were accepted that equilibrium was reached (Figure 1). 50 mL of 400 mg/L Cd(II) or 50 mL of 400 mg/L Pb(II) solution including resin mass (about 50 mg) was mixed at time intervals (15, 30, 45, 60, 90 and 120 min) at 298 or 308 or 318 K temperatures. Concentrations of Cd(II) and Pb(II) ions in eluent solutions were determined by FAAS after filtration of the resin and the necessary dilutions. These studies were repeated three replicate measurements at 298, 308 and 318 K temperatures.

Linearized forms of the Lagergren pseudo first order, pseudo-second order and second order rate equations, respectively were implemented to results found experimentally.

Rate equations can be explained by following equations (9, 10, 11):

The pseudo first order; $(q_e - q_t) = \log q_e - \frac{k_1}{2.303} \cdot t$

(9)

The pseudo-second order; $\frac{t}{q_t} = \frac{1}{k_2 q_e^2} + \left(\frac{1}{q_e}\right) \cdot t$

(10)

The second order; $\frac{1}{(q_e - q_t)} = \frac{1}{q_e} + k \cdot t$

(11)

where, k_1 is the Lagergren pseudo first-order absorption rate constant (1/min), k_2 is Pseudo second order rate constant (g/(mg·min)) and k is second order rate constant at equilibrium (g/(mg·min)). The q_e and q_t are mass of analyte ions per mass of adsorbent (mg/g) at equilibrium and at time t (min), respectively. Plots of t/q_t values versus t were obtained and they were shown in Figure 4 as an example. Rate constants and q_e values obtained from slopes and intercepts for each plot were dedicated in Table 3. As dedicated in Table 3, most appropriate kinetic model for adsorption of Cd(II) and Pb(II) on resin was pseudo second order kinetic model [1-3] because correlation coefficients (R^2 values: 0.9920 - 0.9971) found were highest among other models.

3.5. Contact time and temperature

Contact time and temperature for adsorption of Cd(II) and Pb(II) ions are also important for successful use of adsorbents in applications. Fast adsorption rate may be related to the form and structure of adsorbent. Thus, active adsorption sites may be located at the

outer surface of adsorbent and mass transfer during adsorption process may be neglected [34, 58-62]. For this purpose, effects of contact time and temperature on adsorption of Cd(II) and Pb(II) ions on resin were studied to obtain optimum contact time and temperature conditions for adsorption process by using solutions of Cd(II) and Pb(II). Means of three replicate measurements of results with standard deviation (less than 3%) were obtained. Contact times for adsorption of Cd(II) and Pb(II) ions on resin at 298, 308 and 318 K were depicted in Figure 5. As depicted in Figure 5, adsorption of Cd(II) and Pb(II) ions increased by increasing contact time up to 45 min and after then it was almost constant. Therefore, optimum contact time of analyte ions with the resin was found as 45 min. When temperature of adsorption process by using resin was increased from 298 K to 318 K, adsorption of Cd(II) and Pb(II) decreased. These results demonstrated that adsorption of Cd(II) and Pb(II) on resin was exothermic. By increasing temperature of adsorption process, release of metal ions from interface of adsorbent to solution might increase. Optimum temperature was observed as 298 K [34, 62].

3.6. Activation energies

After determining the kinetics of ion exchange reaction related to adsorption of Cd(II) and Pb(II) ions on Amberlyst 15 resin as pseudo-second-order rate kinetics, activation energies of reactions were obtained by equation (12):

$$\ln k = -\left(\frac{E_a}{R}\right)\frac{1}{T} + \ln A$$

(12)

where, E_a is activation energy (J/mol), T is temperature (K) and R is gas constant. Rate constant values obtained from pseudo second order kinetic for Cd(II) and Pb(II) ions at 298, 308 and 318 K versus to 1/T were plotted and depicted in Figure 6. The activation

energies of Cd(II) and Pb(II) were obtained from slopes of straight lines according to equation (12) and they were given in Table 3.

3.7. Determination of thermodynamic parameters

Adsorption or desorption of metal ions with adsorbent may be explained by reversible reaction as metal ion in solution \rightleftharpoons metal ion on adsorbent at equilibrium.

Apparent equilibrium constant (K'_C) for adsorption based on concentration is clarified by equation (13):

$$K'_C = \frac{C_{ad,e}}{C_e}$$

(13)

where, $C_{ad,e}$ and C_e are equilibrium concentrations of metal ions (mg/L) on the adsorbent and in solution, respectively. Apparent equilibrium constant values (K'_C) were obtained by using equation (13) and $C_{ad,e}$ and C_e values obtained from 50 mL of 400 mg/L Cd(II) or 50 mL of 400 mg/L Pb(II) solutions including about 50 mg Amberlyst 15 given in section 2.3. The studies were repeated three replicate measurements at 298, 308 and 318 K temperatures. Apparent equilibrium constant values (K'_C) versus equilibrium concentrations of Cd(II) and Pb(II) (C_e) in solutions were plotted to obtain thermodynamic equilibrium constant (K_C°). Obtained lines were extrapolated to zero for infinite dilution and thermodynamic equilibrium constant (K_C°) values were found at 298, 308 and 318 K. The K_C° values obtained were means of three replicate measurements of Cd(II) and Pb(II) concentrations in solutions and they were given in Table 4.

Thermodynamic parameters (ΔG° , ΔH° and ΔS°) were obtained by equations (14 and 15):

$$\Delta G^\circ = -RT \ln K_c^\circ = \Delta H^\circ - T \Delta S^\circ \quad (14)$$

$$\ln K_c^\circ = \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{RT} \quad (15)$$

where, K_c° is thermodynamic equilibrium constant, R is gas constant, T is temperature (K), ΔG° is Gibbs standard free energy change for adsorption (kJ/mol), ΔH° is standard enthalpy change (kJ/mol) and ΔS° is standard entropy change (J/(mol·K)). ΔG° shows spontaneity of a chemical reaction. Reaction occurs spontaneously at a given temperature when ΔG° is negative. ΔS° shows disorderliness of adsorption at solid - liquid interface. Gibbs free energy changes for adsorption of Cd(II) and Pb(II) on resin were calculated by utilizing equation (14) and were dedicated in Table 4. As seen in Table 4, all ΔG° values obtained were negative. Negative ΔG° values showed that adsorptions of Cd(II) and Pb(II) ions on resin are feasible and adsorption is spontaneous at three different temperatures. Plots of $\ln K_c^\circ$ versus $1/T$ obtained at 298 K for Cd(II) and Pb(II) ions were depicted in Figure 7. ΔH° and ΔS° changes for Cd(II) and Pb(II) were obtained from slope and intercept of each straight line according to equation (15). The ΔH° and ΔS° values found from the plots were depicted in Table 4. Negative values of enthalpy changes (ΔH°) indicated that adsorptions of Cd(II) and Pb(II) ions on resin were exothermic. Negative values of entropy changes (ΔS°) indicated that randomness between solid and liquid interfaces decreased during adsorption of Cd(II) and Pb(II) ions on Amberlyst 15.

4. Conclusion

Adsorption isotherms, kinetics and thermodynamic parameters for Cd(II) and Pb(II) ions from water solutions were performed by utilizing Amberlyst 15 resin in terms of its availability and adsorptive capacity. The Langmuir model was more suitable than Freundlich adsorption isotherm. Monolayer adsorption capacity of resin was found as 120 mg/g for Cd(II) and 116 mg/g for Pb(II) experimentally at 318 K. According to D-R model, Cd and Pb adsorptions on resin have been a chemical ion exchange process. The batch adsorption method depended on concentration of initial metal, pH value of solution, contact time and temperature was utilized in studies. From kinetic data obtained, adsorptions of Cd(II) and Pb(II) ions on resin were explained by pseudo second order kinetic. Negative values of ΔG° and ΔH° were confirmed that reaction was spontaneous, exothermic and favorable for adsorption of Cd(II) and Pb(II) ions by resin from natural and waste waters. Negative value of ΔS° indicated that the decrease occurred in randomness between solid and liquid interfaces.

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References

1. Ghasemi N, Ahmadi M, Piri A, Ghasemi M, Sillanpää M. Pb (II) adsorption on pumpkin char and modified pumpkin char: optimisation, kinetics, equilibrium and thermodynamics studies. *International Journal of Environmental Analytical Chemistry* 2020. doi: 10.1080/03067319.2020.1766033
2. Şenol ZM, Şimşek S. Equilibrium, kinetics and thermodynamics of Pb(II) ions from aqueous solution by adsorption onto chitosan-dolomite composite beads.

- International Journal of Environmental Analytical Chemistry 2020. doi: 10.1080/03067319.2020.1790546
3. Baran MF, Duz MZ. Removal of cadmium (II) in the aqueous solutions by biosorption of *Bacillus licheniformis* isolated from soil in the area of Tigris River. International Journal of Environmental Analytical Chemistry 2019. doi: 10.1080/03067319.2019.1669583
 4. Karthik R, Meenakshi S. Removal of Pb(II) and Cd(II) ions from aqueous solution using polyaniline grafted chitosan. Chemical Engineering Journal 2014; 263: 168–177. doi: 10.1016/j.cej.2014.11.015
 5. Akinyeye OJ, Ibigbami T, Odeja OO, Sosanolu OM. Evaluation of kinetics and equilibrium studies of biosorption potentials of bamboo stem biomass for removal of Lead (II) and Cadmium (II) ions from aqueous solution. African Journal of Pure and Applied Chemistry 2020; 14 (2): 24–41. doi: 10.5897/AJPAC2019.0812
 6. Tirtom VN, Dinçer A. Effective removal of heavy metals from an aqueous solution with poly(N- vinylimidazoleacrylamide) hydrogels. Separation Science and Technology 2021; 56 (5): 912 – 924. doi: 10.1080/01496395.2020.1735434
 7. Younes AA, Abdulhady YAM, Shahat NS, El-Din El-Dars FMS. Removal of cadmium ions from wastewaters using corn cobs supporting nano-zero valent iron. Separation Science and Technology 2019; 1-2: 1-13. doi: 10.1080/01496395.2019.1708109
 8. Naseri MT, Hemmatkhah P, Hosseini MRM, Assadi Y. Combination of dispersive liquid-liquid micro-extraction with flame atomic absorption spectrometry using microsample introduction for determination of lead in water samples. Analytica Chimica Acta 2008; 610: 135–141. doi: 10.1016/j.aca.2008.01.020

9. Liang P, Sang H. Determination of trace lead in biological and water samples with dispersive liquid-liquid microextraction preconcentration. *Analytical Biochemistry* 2008; 380 (1): 21–25. doi: 10.1016/j.ab.2008.05.008
10. Portugal LA, Ferreira HS, Santos W, Ferreira SLC. Simultaneous pre-concentration procedure for the determination of cadmium and lead in drinking water employing sequential multi-element flame atomic absorption spectrometry. *Microchemical Journal* 2011; 87 (1): 77–80. doi: 10.1016/j.microc.2007.05.008
11. Silva EL, Roldan PS. Simultaneous flow injection preconcentration of lead and cadmium using cloud point extraction and determination by atomic absorption spectrometry. *Journal of Hazardous Materials* 2009; 161 (1): 142–147. doi: 10.1016/j.jhazmat.2008.03.100
12. Ghaedi M, Shokrollahi A, Nikham K, Nikham E, Najibi A et al. Cloud point extraction and flame atomic absorption spectrometric determination of cadmium(II), lead(II), palladium(II) and silver(I) in environmental samples. *Journal of Hazardous Materials* 2009; 168 (2-3): 1022–1027. doi: 10.1016/j.jhazmat.2009.02.130
13. Oymak T, Tokalıoğlu Ş, Yılmaz V, Kartal Ş, Aydın D. Determination of lead and cadmium in food samples by the coprecipitation method. *Food Chemistry* 2009; 113: 1314-1317. doi: 10.1016/j.foodchem.2008.08.064
14. Burham N. Separation and preconcentration system for lead and cadmium determination in natural samples using 2-aminoacetylthiophenol modified polyurethane foam. *Desalination* 2009; 249 (3): 1199–1205. doi: 10.1016/j.desal.2009.04.009

15. Kalfa OM, Yalçinkaya O, Türker AR. Synthesis of nano B₂O₃/TiO₂ composite material as a new solid phase extractor and its application to preconcentration and separation of cadmium. *Journal of Hazardous Materials* 2009; 166: 455–461. doi: 10.1016/j.jhazmat.2008.11.112
16. Xie F, Lin X, Wu X, Xie Z. Solid phase extraction of lead(II), copper(II), cadmium(II) and nickel(II) using gallic acid-modified silica gel prior to determination by flame atomic absorption spectrometry. *Talanta* 2007; 74 (4): 836–843. doi: 10.1016/j.talanta.2007.07 .018
17. Parham H, Pourreza N, Rahbar N. Solid phase extraction of lead and cadmium using solid sulfur as a new metal extractor prior to determination by flame atomic absorption spectrometry. *Journal of Hazardous Materials* 2008; 163 (2-3): 588–592. doi: 10.1016/j.jhazmat. 2008.07.007
18. Ciftci H. Separation and solid phase extraction method for the determination of cadmium in environmental samples. *Desalination* 2010; 263 (1): 18–22. doi: 10.1016/j.desal. 2010.06.028
19. Baytak S, Kendüzler E, Türker AR. Separation/preconcentration of Zn(II), Cu(II) and Cd(II) by *Saccharomyces carisbergensis* immobilized on silica gel 60 in various samples. *Separation Science and Technology* 2006; 41: 3449–3465. doi: 10.1080/ 01496390600915098
20. Jagirani MS, Soylok M. A review: Recent advances in solid phase microextraction of toxic pollutants using nanotechnology scenario. *Microchemical Journal* 2020; 159: 105436. doi: 10.1016/j.microc.2020.105436
21. Ngah WSW, Fatinathan S. Pb(II) biosorption using chitosan and chitosan derivatives beads: Equilibrium, ion Exchange and mechanism studies. *Journal of*

- Environmental Science 2010; 22 (3): 338–346. doi: 10.1016/s1001-0742(09)60113-3
22. Pehlivan E, Altun T. The study of various parameters affecting the ion Exchange of Cu^{2+} , Zn^{2+} , Ni^{2+} , Cd^{2+} and Pb^{2+} from aqueous solution on Dowex 50W synthetic resin. Journal of Hazardous Materials 2006; 134 (1-3): 149–156. doi: 10.1016/j.jhazmat.2005.10.052
 23. Maltez HF, Borges DL, Carasek E, Welz B, Curtis AJ. Single drop micro-extraction with O, O-diethyl dithiophosphate for the determination of lead by electrothermal atomic absorption spectrometry. Talanta 2008; 74 (4): 800–805. doi: 10.1016/j.talanta.2007.07.010
 24. Yang B, Gong Q, Zhao L, Sun H, Ren N et al. Preconcentration and determination of lead and cadmium in water samples with a MnO_2 coated carbon nanotubes by using ETAAS. Desalination 2011; 278: 65–69. doi: 10.1016/j.desal.2011.05.010
 25. Kummrow F, Silva FF, Kuno R, Souza AL, Oliveira PV. Biomonitoring method for the simultaneous determination of cadmium and lead in whole blood by electrothermal atomic absorption spectrometry for assessment of environmental exposure. Talanta 2008; 75: 246–252. doi: 10.1016/j.talanta.2007.11.003
 26. Maranhão TA, Martendal E, Borges DLG, Carasek E, Welz B et al. Cloud point extraction for the determination of lead and cadmium in urine by graphite furnace atomic absorption spectrometry with multivariate optimization using Box-Behnken design. Spectrochimica Acta Part B 2007; 62 (9): 1019–1027. doi: 10.1016/j.sab.2007.05.008
 27. Trujillo I, Alonso E, Pavón J. Development of a solid phase extraction method for the multielement determination of trace metals in natural waters including sea-

- water by FI-ICP-MS. *Microchemical Journal* 2012; 101: 87–94. doi: 10.1016/J.MICROC.2011.11.003
28. Dong L, Zhu Z, Ma H, Qui Y, Zhao J. Simultaneous adsorption of lead and cadmium on MnO₂-loaded resin. *Journal of Environmental Science* 2010; 22 (2): 225–229. doi: 10.1016/S1001-0742(09)60097-8
29. Rao KS, Chaudhury GR, Mishra BK. Kinetics and equilibrium studies for the removal of cadmium ions from aqueous solutions using Duolite ES 467 resin. *International Journal of Mineral Processing* 2010; 97 (1-4): 68-73. doi: 10.1016/j.minpro.2010.08.003
30. Türker AR. Separation, preconcentration and speciation of metal ions by solid phase extraction. *Separation and Purification Review* 2012; 41 (3): 169–206. doi: 10.1080/15422119.2011.585682
31. Türker AR. New sorbents for solid-phase extraction for metal enrichment. *Clean-Soil Air Water* 2007; 35: 548–557. doi: 10.1002/clen.200700130
32. Öztürk Ş, Aslım B, Türker AR. Removal of cadmium ions from aqueous samples by *Synechocystis sp.* *Separation Science and Technology* 2009; 44: 1467–1483. doi: 10.1080/01496390902766124
33. Subbaiah MV, Gutha Y, Vijiya Y, Krishnaiah A. Equilibrium, kinetic and thermodynamic studies on biosorption of Pb(II) and Cd(II) from aqueous solution by fungus (*Trametes versicolor*) biomass. *Journal of Taiwan Institute of Chemical Engineers* 2011; 42: 965–971. doi: 10.1016/J.JTICE.2011.04.007
34. Sarı A, Tüzen M. Kinetic and equilibrium studies of biosorption of Pb(II) and Cd(II) from aqueous solution by macrofungus (*Amanita rubescens*) biomass.

- Journal of Hazardous Materials 2009; 164: 1004–1011. doi: 10.1016/j.jhazmat.2008.09.002
35. Zheng L, Dang Z, Yi X, Zhang H. Equilibrium and kinetic studies of adsorption of Cd(II) from aqueous solution using modified corn stalk. Journal of Hazardous Materials 2010; 176 (1-3): 650–656. doi: 10.1016/j.jhazmat.2009.11.081
36. Lasheen MR, Ammar NS, Ibrahim HS. Adsorption/desorption of Cd(II), Cu(II) and Pb(II) using chemically modified orange peel: Equilibrium and kinetic studies. Solid State Science 2012; 14 (2): 202–210. doi: 10.1016/j.solidstatesciences.2011.11.029
37. Gupta VK, Rastogi A. Biosorption of lead from aqueous solutions by green algae *Spirogyra* species: Kinetics and equilibrium studies. Journal of Hazardous Materials 2008; 152 (1): 407–414. doi: 10.1016/j.jhazmat.2007.07.028
38. Yalçinkaya O, Kalfa OM, Türker AR. Preconcentration of trace copper, cobalt and lead from various samples by hybrid nano sorbent and determination by FAAS. Current Analytical Chemistry 2011; 7 (3): 225–234. doi: 10.2174/1573411011107030225
39. Yalçinkaya O, Kalfa OM, Türker AR. Chelating agent free- solid phase extraction (CAF-SPE) of Co(II), Cu(II) and Cd(II) by new nano hybrid material (ZrO₂/B₂O₃). Journal of Hazardous Materials 2011; 195: 332–339. doi: 10.1016/j.jhazmat.2011.08.048
40. Jeon W, Ban C, Kim JE, Woo HC, Kim DH. Production of furfural from macroalgae-derived alginic acid over Amberlyst – 15. Journal of Molecular Catalysis A-Chemical 2016; 423: 264–269. doi: 10.1016/j.molcata.2016.07.020

41. Razzaq R, Shah KH, Fahad M, Naeem A, Sherazi TA. Adsorption potential of macroporous Amberlyst-15 for Cd(II) removal from aqueous solutions. *Material Research Express* 2020; 7 (2): 025509. doi: 10.1088/2053-1591/ab6e7a
42. Otremska P, Gega J. Kinetic studies on sorption of Ni(II) and Cd(II) from chloride solutions using selected acidic cation exchangers. *Physicochemical Problems of Mineral. Processing* 2013; 49 (1): 301–312. doi: 10.5277/ppmp130127
43. Tunçeli A, Ulaş A, Acar O, Türker AR. Solid phase extraction of cadmium and lead from water by amberlyst 15 and determination by flame atomic absorption spectrometry. *Bulletin of Environmental Contamination and Toxicology* 2018; 102: 297–302. doi: 10.1007/s00128-018-2498-y
44. Tunçeli A, Yalçinkaya Ö, Türker AR. Solid phase extraction of Pb(II) in water samples on amberlyst 36 and determination of the equilibrium, kinetic and thermodynamic parameters of the adsorption. *Current Analytical Chemistry* 2013; 9 (3): 513–521. doi: 10.274/1573411011309030021
45. Feng Y, Gong JL, Zeng GM, Niu QY, Zhang HY et al. Adsorption of Cd(II) and Zn (II) from aqueous solutions using magnetic hydroxyapatite nanoparticles as adsorbents. *Chemical Engineering Journal* 2010; 162: 487–494. doi: 10.1016/j.cej.2010.05.049
46. Mustapha S, Shuaib DT, Ndamitso MM, Etsuyankpa MB, Sumaila A et al. Adsorption isotherm, kinetic and thermodynamic studies for the removal of Pb(II), Cd(II), Zn(II) and Cu(II) ions from aqueous solutions using *Albizia lebbbeck* pods. *Applied Water Science* 2019; 9 (6): Article number: 142. doi: 10.1007/s13201-019-1021-x

47. Malik UR, Hasany SM, Subhani MS. Sorptive potential of sunflower stem for Cr(III) ions from aqueous solutions and its kinetic and thermodynamic profile. *Talanta* 2005; 66 (1): 166–173. doi: 10.1016/j.talanta.2004.11.013
48. Goel J, Kadirvelu K, Rajagopal C, Garg VK. Removal of lead (II) by adsorption using treated granular activated carbon: Batch and column studies. *Journal of Hazardous Materials* 2005; 125: 211-220. doi: 10.1016/j.jhazmat.2005.05.032
49. Younes AA, Abdulhady YAM, Shahat NS, El-Din El-Dars FMS. Removal of cadmium ions from wastewaters using corn cobs supporting nano-zero valent iron. *Separation Science and Technology* 2021; 56 (1): 1-13. doi: 10.1080/01496395.2019.1708109
50. Bagheri S, Amini MM, Behbahani M, Rabiee G. Low cost thiol-functionalized mesoporous silica, KIT-6-SH, as A useful adsorbent for cadmium ions removal: A study on the adsorption isotherms and kinetics of KIT-6-SH. *Microchemical Journal* 2019; 145: 460–469. doi: 10.1016/j.microc.2018.11.006
51. Karim MR, Aijaz MO, Alharth NH, Alharbi HF, Al-Mubaddel FS et al. Composite nanofibers membranes of poly(vinyl Alcohol)/chitosan for selective lead(II) and cadmium- (II) ions removal from wastewater. *Ecotoxicology and Environmental Safety* 2019; 169: 479–486. doi: 10.1016/j.ecoenv.2018.11.049
52. Zhou N, Wang Y, Yao D, Li S, Tang J et al. Novel wet pyrolysis providing simultaneous conversion and activation to produce surface-functionalized biochars for cadmium remediation. *Journal of Cleaner Production* 2019; 221: 63–72. doi: 10.1016/j.jclepro.2019.02.176

53. Luo M, Lin H, Hea Y, Lia B, Donga Y et al. Efficient simultaneous removal of cadmium and arsenic in aqueous solution by titanium-modified ultrasonic biochar. *Bioresour. Technology* 2019; 284: 333–339. doi: 10.1016/j.biortech. 2019.03.108
54. Nyairo WN, Eker YR, Kowenje C, Akin I, Bingol H et al. Efficient adsorption of lead (II) and copper (II) from aqueous phase using oxidized multiwalled carbon nanotubes/polypyrrole composite. *Separation Science and Technology* 2018; 53 (10); 1498 – 1510. doi: 10.1080/01496395.2018.1424203
55. Kabbashi NA, Atieh MA, Mamun AA, Mirghami MES, Alam MDZ et al. Kinetic adsorption of application of carbon nanotubes for Pb(II) removal from aqueous solution. *Journal of Environmental Science* 2009; 21; 539–544. doi: 10.1016/S1001-0742(08)62305-0
56. Tofiqhy MA, Mohammadi T. Adsorption of divalent heavy metal ions from water using carbon nanotube sheets. *Journal of Hazardous Materials* 2011; 185: 140–147. doi: 10.1016/j.jhazmat.2010.09.008
57. Karthik R, Meenakshi S. Synthesis, characterization and Cr(VI) uptake study of polyaniline coated chitin. *International Journal of Biological Macromolecules* 2015; 72: 235–242. doi: 10.1016/j.ijbiomac.2014.08.022
58. Deng S, Wang P, Zhang G, Dou Y. Polyacrylonitrile-based fiber modified with thiosemicarbazide by microwave irradiation and its adsorption behavior for Cd(II) and Pb(II). *Journal of Hazardous Materials* 2016; 307: 64–72. doi: 10.1016/j.jhazmat. 2016.01.002
59. Chu L, Liu C, Zhou G, Xu R, Tang Y et al. A double network gel as low cost and easy recycle adsorbent: Highly efficient removal of Cd(II) and Pb(II) pollutants

- from wastewater. *Journal of Hazardous Materials* 2015; 300: 153–160. doi: 10.1016/j.jhazmat.2015.06.070
60. Wang F, Lu X, Yan Li -X. Selective removals of heavy metals (Pb^{2+} , Cu^{2+} , and Cd^{2+}) from wastewater by gelation with alginate for effective metal recovery. *Journal of Hazardous Materials* 2016; 308: 75–83. doi: 10.1016/j.jhazmat.2016.01.021
61. Karatas M. Removal of Pb(II) from water by natural zeolitic tuff: Kinetics and thermodynamics. *Journal of Hazardous Materials* 2012; 199–200: 383–389. doi: 10.1016/j.jhazmat.2011.11.035
62. Xiong C, Wang W, Tan F, Luo F, Chen J et al. Investigation on the efficiency and mechanism of Cd(II) and Pb(II) removal from aqueous solutions using MgO nanoparticles. *Journal of Hazardous Materials* 2015; 299: 664–674. doi: 10.1016/j.jhazmat.2015.08.008

Table 1. The isotherm parameters of Cd(II) and Pb(II) obtained from linearized Langmuir, Freundlich and D-R isotherms at different temperatures (T).

Element	T (K)	q_e	Langmuir Model			Freundlich Model			D-R Model		
			q_m (mg/g)	K_L (L/mg)	R^2	K_F (mg/g)	n	R^2	q_m (mg/g)	E (kJ/mol)	R^2
Cd	298	149	152	0.038	0.999	22.2	3.21	0.937	273	12.31	0.971
	308	135	137	0.045	0.999	21.9	3.33	0.918	247	12.91	0.957
	318	120	121	0.039	0.999	20.3	3.67	0.892	213	13.36	0.938
Pb	298	152	154	0.028	0.992	25.9	3.60	0.934	261	13.61	0.962
	308	139	141	0.034	0.996	26.2	3.78	0.927	236	14.43	0.955
	318	116	116	0.040	0.998	24.0	3.99	0.895	197	15.08	0.935

Table 2. A comparison of adsorption capacities of adsorbent in this study with literature values

Metal	Adsorbent	Adsorption capacity q_m (mg/g)	References
Cd (II)	Corn cobs supporting nano-zero valent iron	145.0	[49]
	Thiol-functionalized mesoporous silica	85.0	[50]
	Composite nano fibers membranes of poly(vinyl alcohol)/chitosan	148.8	[51]
	Surface-functionalized biochars	197.0	[52]
	Titanium-modified ultrasonic biochar	72.62	[53]
	Amberlyst 15 resin	121 - 152	This study
Pb (II)	oMWCNT/Ppy	26.32	[54]
	CNTs	102.04	[55]
	Oxidized MWCNTs	117.6	[56]
	Amberlyst 15 resin	116 - 154	This study

Table 3. Pseudo first order, pseudo second order and second order parameters for adsorption of Cd(II) and Pb(II) at different temperatures (T).

Element	T (K)	Pseudo first order			Pseudo second order			Second order		
		q_e (mg/g)	k_1 (1/min)	R^2	q_e (mg/g)	k_2 (g/min·mg)	R^2	q_e (mg/g)	k (g/min·mg)	R^2
Cd	298	80.9	0.0324	0.8985	138.9	1.69×10^{-3}	0.9968	500.0	0.0018	0.9932
	308	75.6	0.0373	0.9177	125.0	1.97×10^{-3}	0.9971	95.2	0.0030	0.9839
	318	57.7	0.0318	0.8713	103.1	2.41×10^{-3}	0.9967	416.7	0.0024	0.9678
Pb	298	84.0	0.033	0.8984	123.5	1.48×10^{-3}	0.9914	45.1	0.0027	0.7538
	308	78.6	0.033	0.8796	120.5	1.66×10^{-3}	0.9920	40.8	0.0030	0.7414
	318	63.4	0.030	0.9002	101.0	1.93×10^{-3}	0.9932	147	0.0023	0.8443

Table 4. Thermodynamic parameters of Cd(II) and Pb(II) adsorption on Amberlyst 15 at three different temperatures.

Element	Temperature (K)	K_C°	ΔG° (kJ/mol)	ΔH° (kJ/mol)	ΔS° (J/(mol·K))	E_a (kJ/mol)
Cd	298	1.8	-1.5			
	308	1.7	-1.4	-6.2	-16	13
	318	1.6	-1.2			
Pb	298	1.7	-1.4			
	308	1.7	-1.4	-4.1	- 8.9	9.8
	318	1.6	-1.2			

Captions of figures

Figure 1. Effects of initial concentrations of Cd(II) and Pb(II) on adsorption (Sample volume: 50 mL, pH: 4).

Figure 2. Linearized Langmuir isotherms related to adsorptions of Cd(II) and Pb(II).

Figure 3. Linearized form of D-R isotherm for Cd(II) and Pb(II).

Figure 4. Lagergren's pseudo-second order kinetic model for Cd(II) and Pb(II).

Figure 5. Effects of contact time and temperature for adsorption of Cd(II) and Pb(II) on Amberlyst 15 resin at pH 4.0.

Figure 6. Plots of $\ln k$ versus $1/T$ for Cd(II) and Pb(II).

Figure 7. Plots of $\ln K_C^\circ$ versus $1/T$ for Cd(II) and Pb(II).

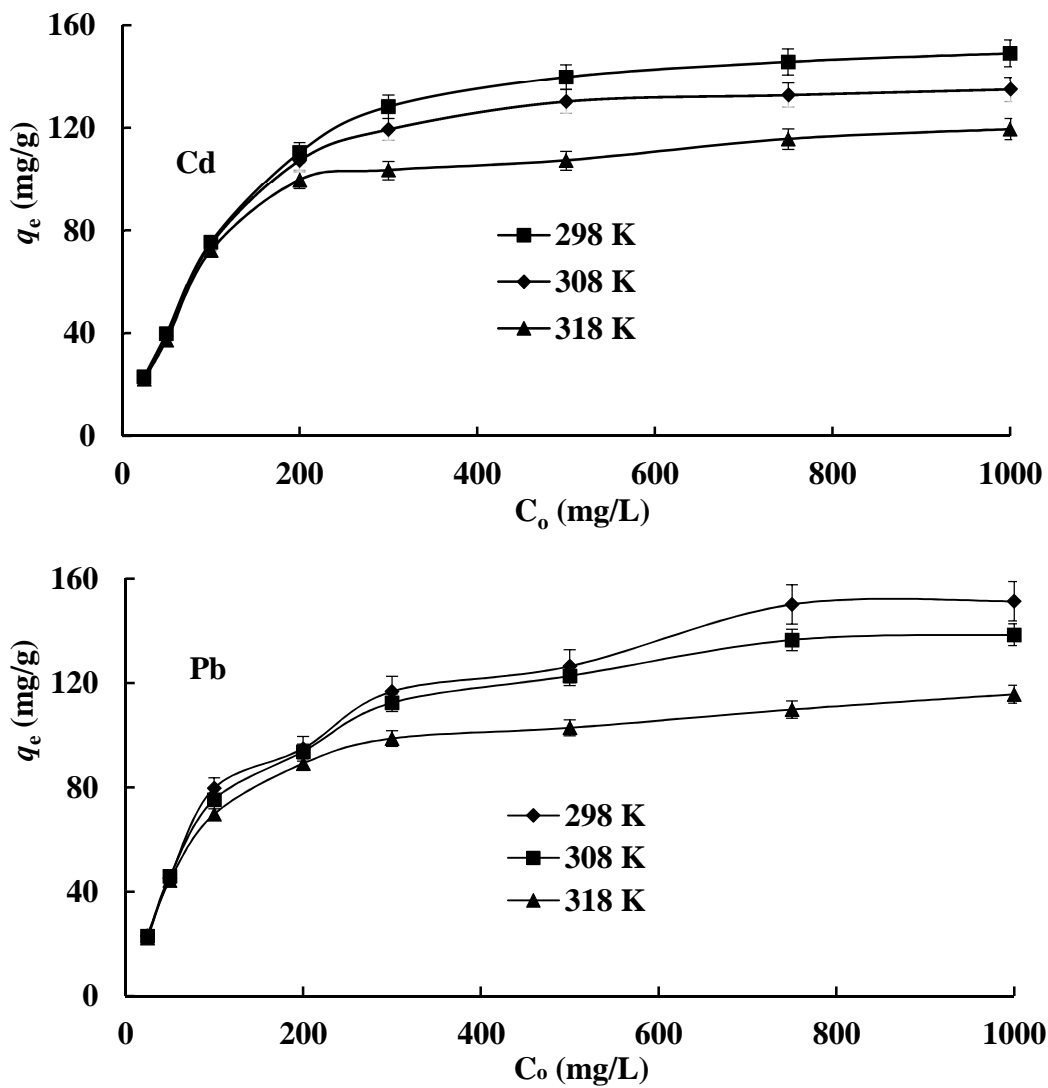


Figure 1. Effects of initial concentrations of Cd(II) and Pb(II) on adsorption (Sample volume: 50 mL, pH: 4).

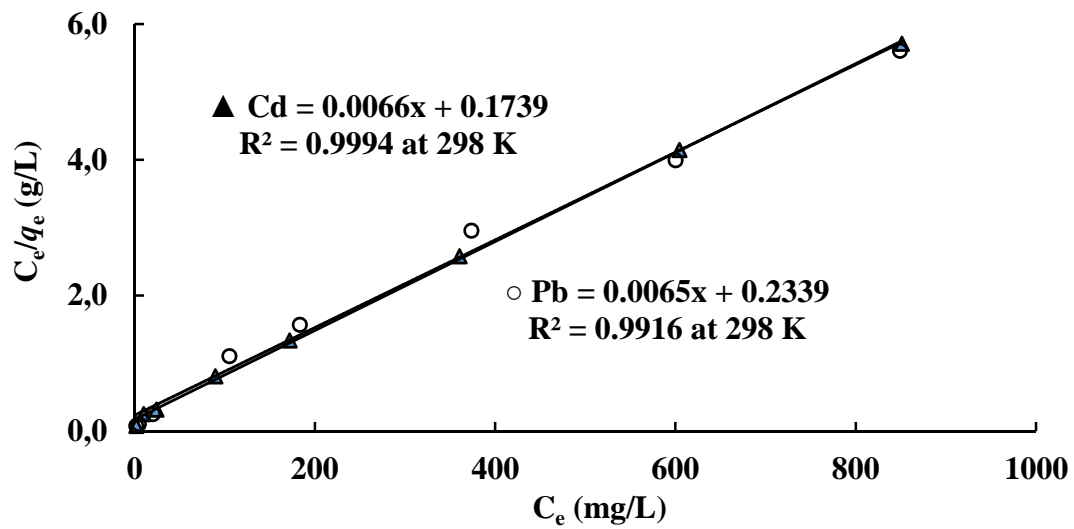


Figure 2. Linearized Langmuir isotherms related to adsorptions of Cd(II) and Pb(II).

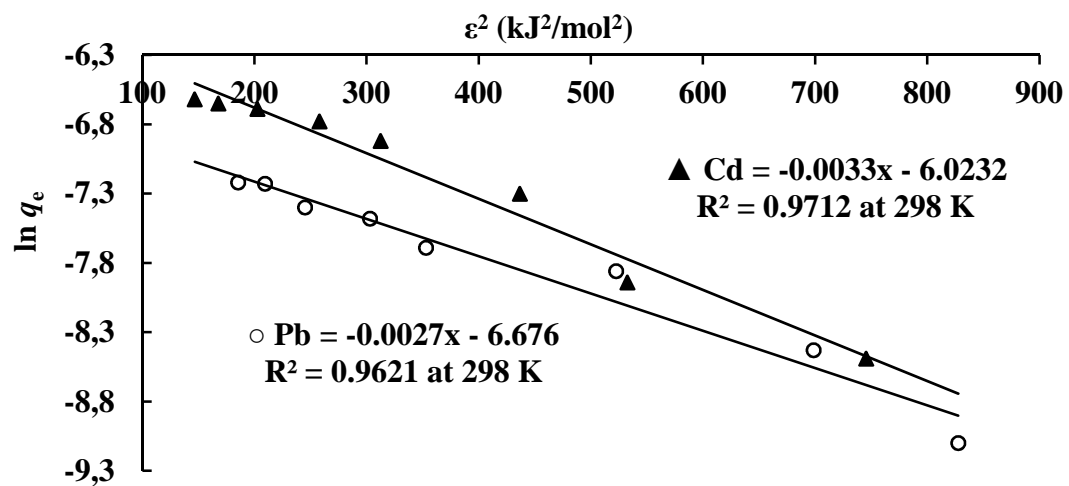


Figure 3. Linearized form of D-R isotherm for Cd(II) and Pb(II).

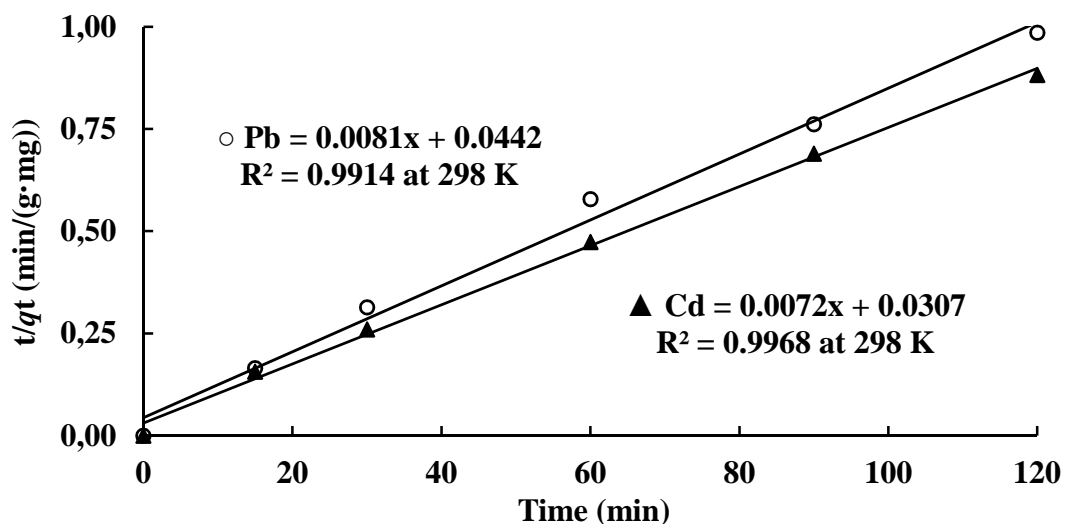


Figure 4. Lagergren's pseudo-second order kinetic model for Cd(II) and Pb(II).

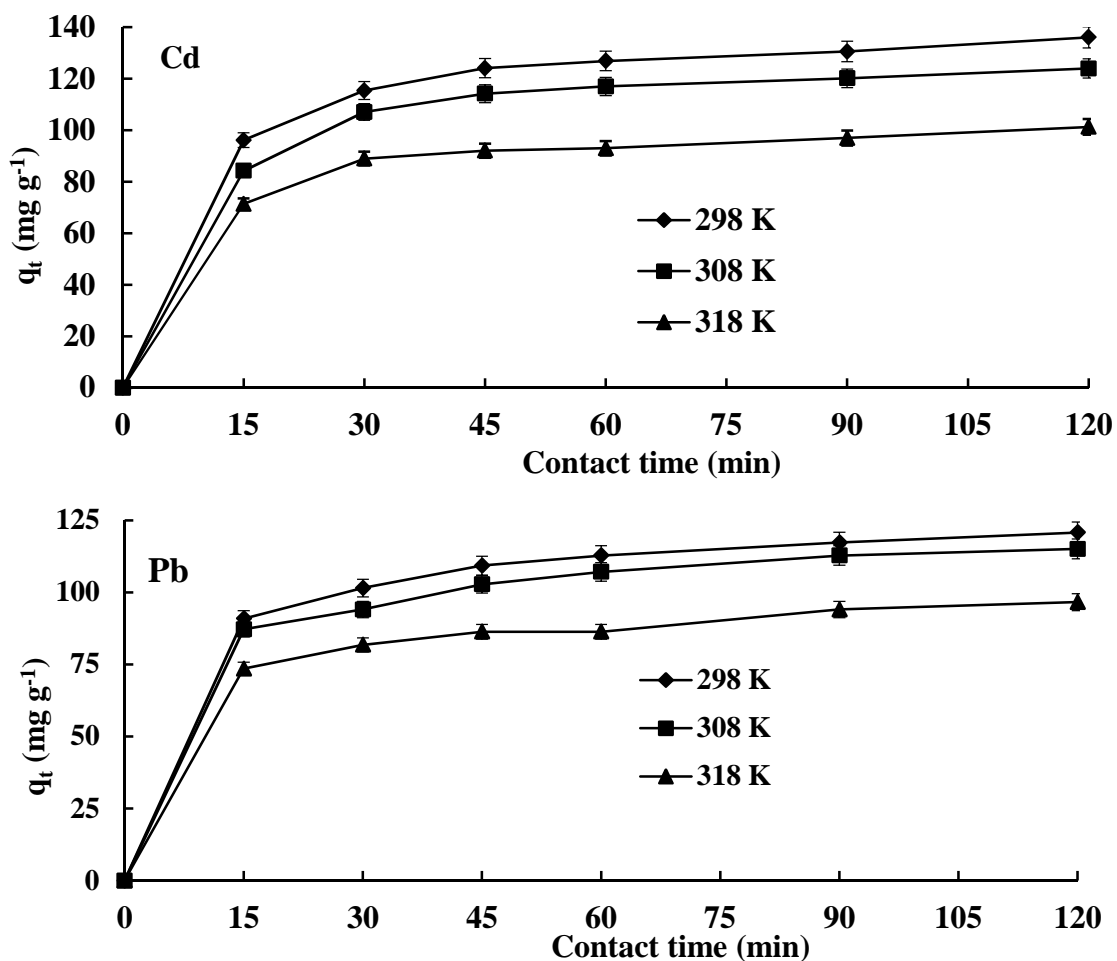


Figure 5. Effects of contact time and temperature for adsorption of Cd(II) and Pb(II) on Amberlyst 15 resin at pH 4.0.

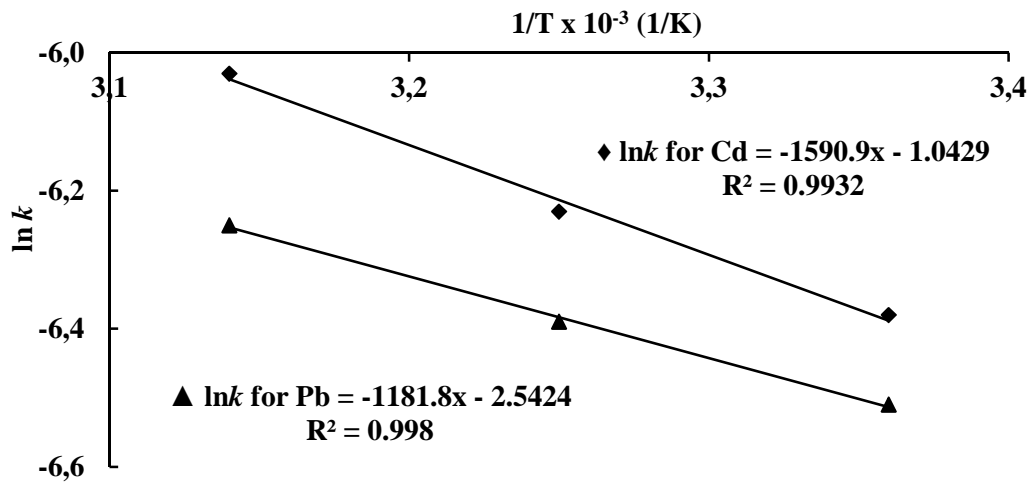


Figure 6. Plots of $\ln k$ versus $1/T$ for Cd(II) and Pb(II).

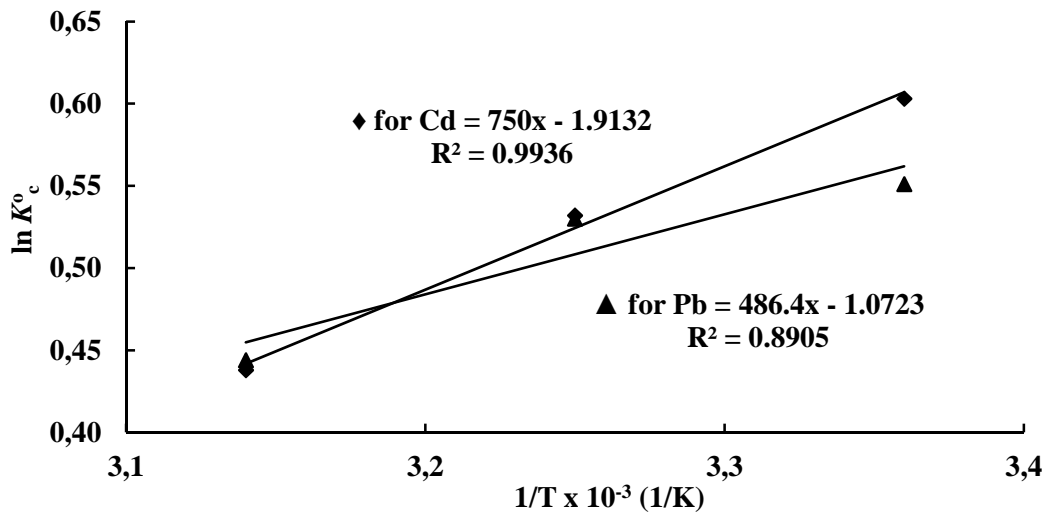


Figure 7. Plots of $\ln K^{\circ}_c$ versus $1/T$ for Cd(II) and Pb(II).